

## 2.1 DEFINING AVERAGE AND INSTANTANEOUS RATES OF CHANGE AT A POINT

1. The average rate of change over an interval becomes a better and better estimate as we \_\_\_\_\_ the interval, until eventually, when we narrow the interval to 0, the \_\_\_\_\_ rate of change will equal the \_\_\_\_\_ rate of change.
2. Give an equivalent expression for the difference quotient.

$$\frac{f(x) - f(a)}{x - a} =$$

## 2.2 DEFINING THE DERIVATIVE OF A FUNCTION AND USING DERIVATIVE NOTATION

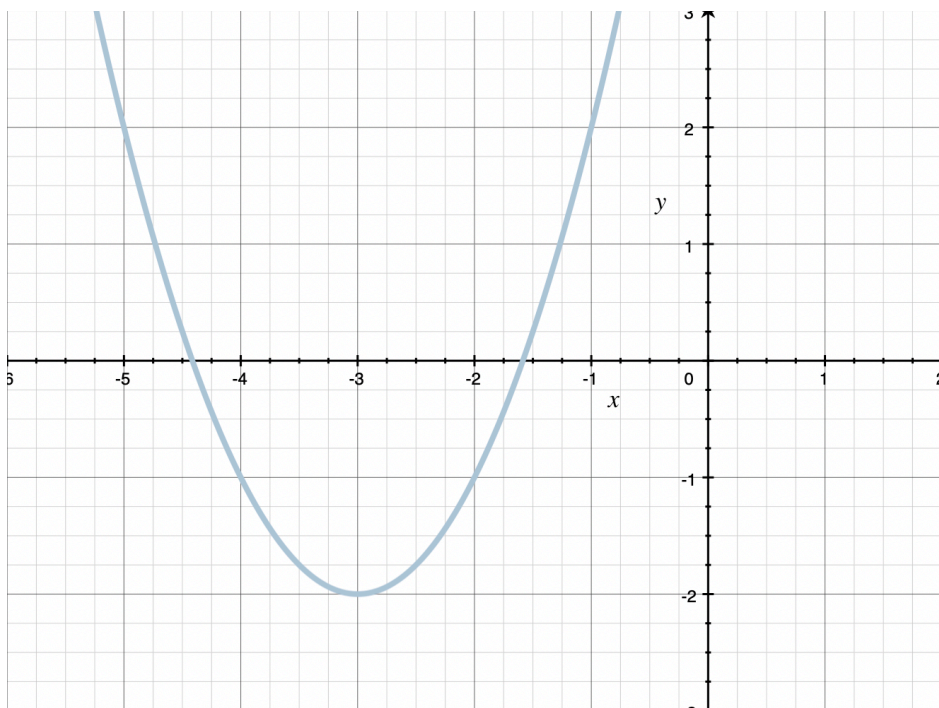
1. Give other expressions for the derivative.
2. Write an expression for instantaneous rate of change at  $x = a$ .
3. The \_\_\_\_\_ at a point is equal to the \_\_\_\_\_ of the \_\_\_\_\_ line at that point.

## 2.3 ESTIMATING DERIVATIVES OF A FUNCTION AT A POINT

1. Use the table to estimate the derivative of  $f(x)$  at  $x = 3.5$ .

$x$	1	2	3	4	5
$f(x)$	-3	4	2	5	-1

2. Use values near  $x = -2$  from the graph to estimate the derivative of the function at  $x = -2$ .



## 2.4 CONNECTING DIFFERENTIABILITY AND CONTINUITY: DETERMINING WHEN DERIVATIVES DO AND DO NOT EXIST

1. If a function is \_\_\_\_\_ at a point, then it's \_\_\_\_\_ there, but even if a function is \_\_\_\_\_ at a point, it's not necessarily \_\_\_\_\_ there.
2. Name two conditions for differentiability.

## 2.5 APPLYING THE POWER RULE

1. Use power rule to give the derivative of each power function.

$-6x$

$4x^2$

$3x^0$

$-\pi x^{-3}$

## 2.6 DERIVATIVE RULES: CONSTANT, SUM, DIFFERENCE, AND CONSTANT MULTIPLE

1. Find the derivative of each constant.

$3$

$-7$

$\pi^2$

$3e$

2. Find the derivative of each polynomial.

$3x^2 - 6x + 4$

$8\pi^4 - 2x^3 + 6x^{-1}$

## 2.7 DERIVATIVES OF $\cos x$ , $\sin x$ , $e^x$ , AND $\ln x$

1. Complete the table with the derivative of each function.

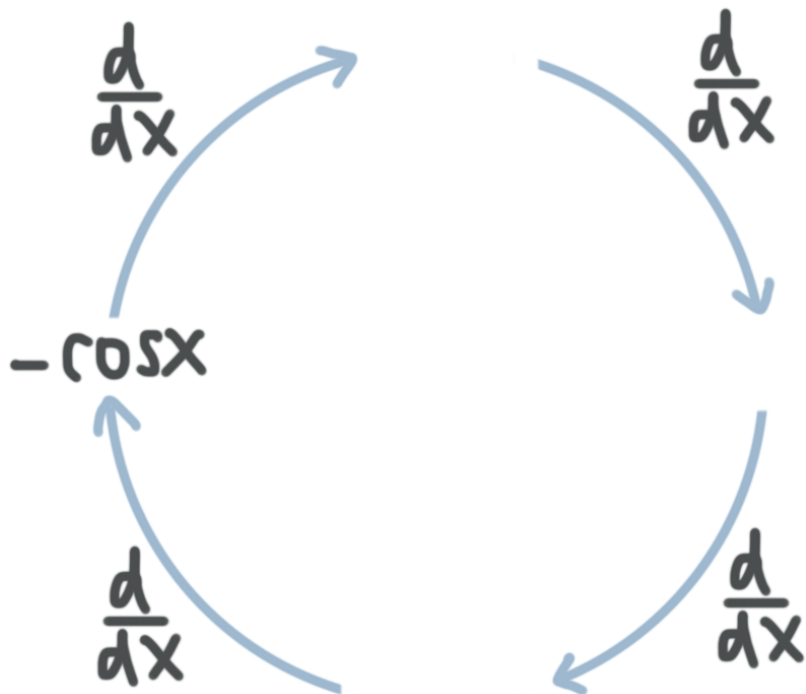
$\sin x$

$e^x$

$\cos x$

$\ln x$

2. Complete the circle diagram with each derivative.



## 2.8 THE PRODUCT RULE

1. Use product rule to differentiate each function.

$$f(x) = g(x)h(x)$$

$$f(x) = e^x \sin x$$

$$f(x) = x^{-3} \ln x$$

2. If the table gives values of the differentiable functions  $f$  and  $g$  and their derivatives at selected values of  $x$ , and if  $h$  is the function defined by  $h(x) = -3g(x) + f(x)g(x)$ , find  $h'(2)$ .

$x$	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
1	1	4	2	-2
2	-3	1	1	-3

## 2.9 THE QUOTIENT RULE

1. If  $s(t) = x(t)/r(t)$ , what is  $s'(t)$ ?
2. Use quotient rule to find the derivative of each rational function.

$$f(x) = \frac{\sin x - e^x}{4x^2}$$

$$g(x) = \frac{9x \ln x}{x + 1}$$

## 2.10 FINDING THE DERIVATIVES OF TANGENT, COTANGENT, SECANT, AND/OR COSECANT FUNCTIONS

1. Re-order the derivatives, below, to line up with the corresponding trig functions, above.

$\sin x$	$\cos x$	$\tan x$	$\csc x$	$\sec x$	$\cot x$
$\sec^2 x$	$\sec x \tan x$	$-\csc^2 x$	$\cos x$	$-\sin x$	$-\csc x \cot x$

2. Use trig identities to prove the derivative of  $\cot x$ .